

# ТЕОРИЯ ИНЖЕНЕРНЫХ СООРУЖЕНИЙ. СТРОИТЕЛЬНЫЕ КОНСТРУКЦИИ

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## ГИПОТЕЗЫ О ДЕПЛАНАЦИИ СЕЧЕНИЯ ОТ ДЕФОРМАЦИЙ СДВИГА В ЖЕЛЕЗОБЕТОННЫХ КОНСТРУКЦИЯХ, ИСПЫТЫВАЮЩИХ КРУЧЕНИЕ С ИЗГИБОМ

**Аннотация.** В статье проведен анализ гипотез о депланации угловых деформаций в железобетонных конструкциях при изгибе с кручением. Рассмотрен простой способ из семейства методов сеток для аппроксимации деформаций сложных функций при рассматриваемом сложном напряженном состоянии. Построены и проанализированы эпюры угловых и линейных деформаций в таких конструкциях для нахождения этих деформаций, изгибающих и крутящих моментов воспринимаемых бетоном сжатой области с использованием принятых гипотез и коэффициентов для проектирования нормальных и касательных напряжений (деформаций) посредством диаграмм сжатого бетона и рабочей арматуры. Аппроксимацией расчетного сечения малыми квадратами построена пространственная поверхность деформаций, с соответствующими градиентами этих деформаций в сечении с трещиной и на этой основе записаны выражения для суммарных продольных деформаций и деформаций сдвига в сечении элемента при изгибе с кручением. С использованием мембранный аналогии функций напряжений Тимошенко-Гудьера и предложенного варианта новых сложных функций из семейства метода сеток проведен анализ погрешности нахождении значения сложных функций в рассмотренных характерных точках (2%) и в любых точках поперечного сечения (7%).

Использование предложенных гипотез и приведенного варианта сложных функций позволяет учитывать депланацию сложнонапряженного сечения железобетонного элемента с трещинами, испытывающего изгиб с кручением.

**Ключевые слова:** билинейная поверхность, опасная пространственная трещина, деформационный эффект железобетона, депланация, градиент, векторы, фибры, форма эпюры.

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## DEPLANATION HYPOTHESES FOR ANGULAR DEFORMATIONS IN REINFORCED CONCRETE STRUCTURES UNDER COMBINED TORSION AND BENDING

**Abstract.** The article analyzes the hypothesis of deplanation of angular deformations in reinforced concrete structures during bending with torsion. A simple method from the field of the grid methods for approximating the deformations of complex functions under the 3D stress state is considered. Diagrams of angular and linear deformations in such structures were built and analyzed to find these deformations, bending and torques perceived by the concrete of the compressed area using the accepted hypotheses and coefficients for projecting normal and shear stresses (strains) through diagrams of compressed concrete and working reinforcement. Approximating the calculated section by small squares, a spatial surface of deformations was constructed. This is with the corresponding gradients of these deformations in the section with a crack, and on this basis, expressions were written for the total longitudinal deformations in the section and shear deformations in the section of the element during bending with torsion. Using the membrane analogy of the Timoshenko-Goodyear stress

*functions and the proposed version of new complex functions from the field of the grid method, an analysis was made of its error, when we find the value of complex functions at the considered characteristic points (2%) and at any points of the cross section (7%).*

*The use of the proposed hypotheses and the given version of complex functions makes it possible considering the warping of the 3D stressed section of a reinforced concrete element with cracks undergoing bending with torsion.*

**Keywords:** bilinear surface, dangerous spatial crack, deformation effect of reinforced concrete, deplanation, delta jump functions, vectors, fibers.

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